

MEG2008 データ解析:

$\mu \rightarrow e\gamma$ 解析

東大素粒子物理国際研究センター

澤田 龍

他、MEGコラボレーション

2009年09月10日

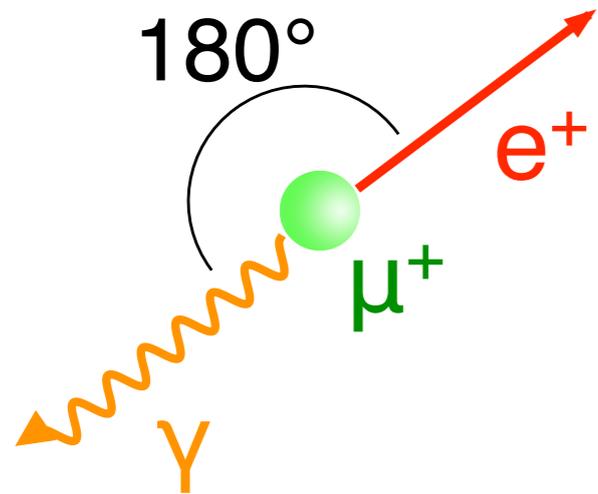
日本物理学会 2009年秋季大会

甲南大学

μ e
 γ

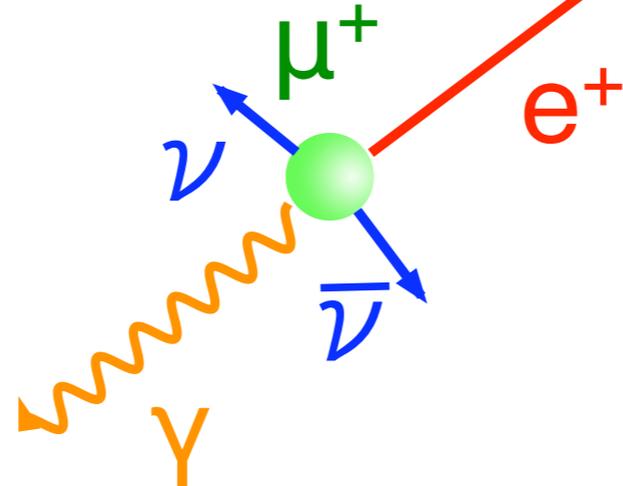
Signal and Background

Signal



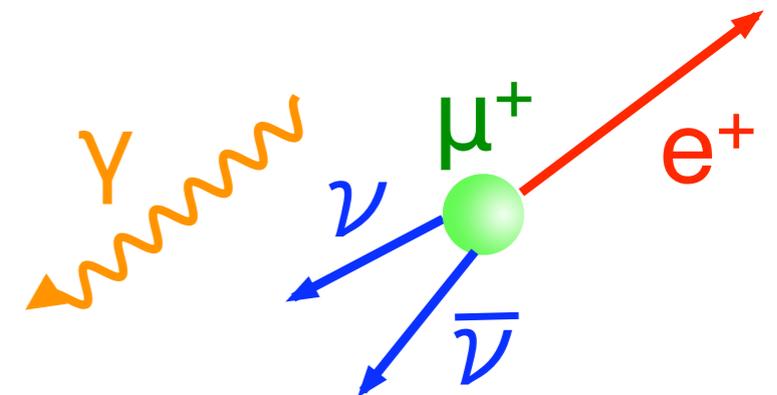
RMD

Radiative muon decay



BG

Accidental pileup



Back-to-Back	Any angle (Energy correlated)	Any angle
52.8 MeV	< 52.8 MeV	< 52.8 MeV *
Same time	Same time	Flat time difference

E_γ

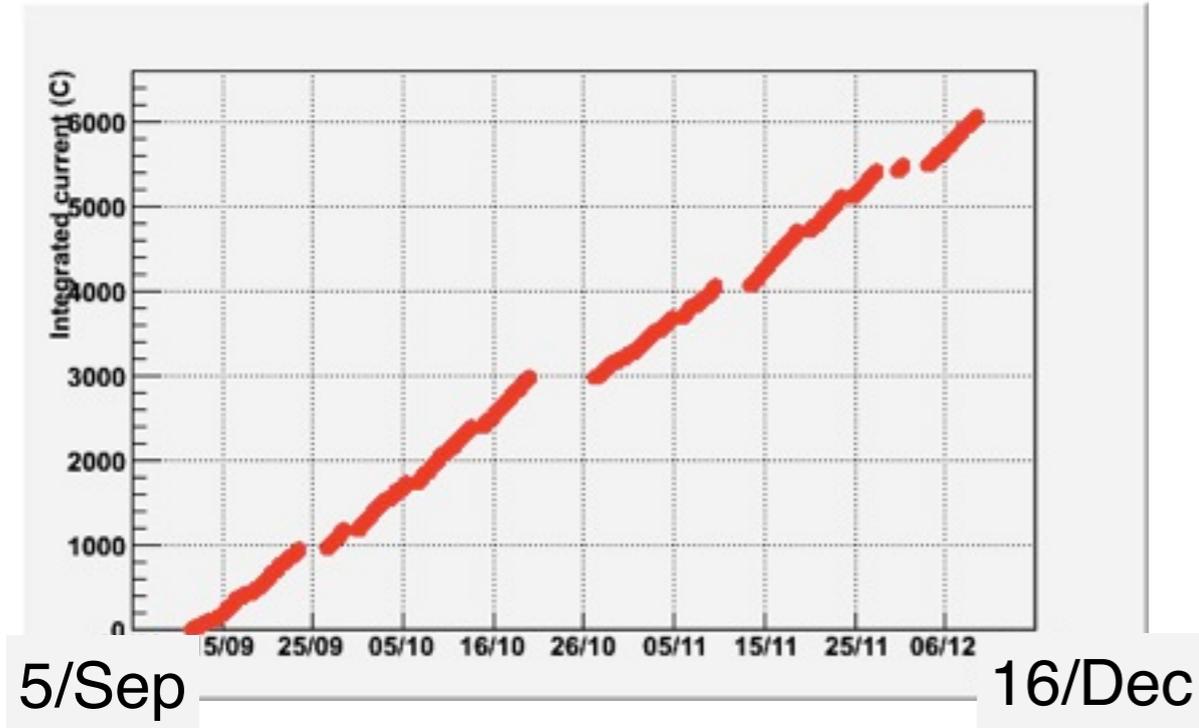
E_{e^+}

T

$\phi \quad \theta$

* Measured E_γ can be larger than signal in the case of pileup of two γ s.

2008 data



- The first three months of MEG experiment
- 3×10^7 muons/sec rate, in total 9.5×10^{13} muons stopped on the target.
- Physics run

Event rate	4.6 event/sec
DAQ time	4.0 Msec
# triggered events	21.7 M *
Data size	1.5 MB/event
Total data size	31TB *

- Condition was not the best
 - DCH discharge (low efficiency and resolution.)
 - TC fiber not in operation. (lower trigger efficiency)

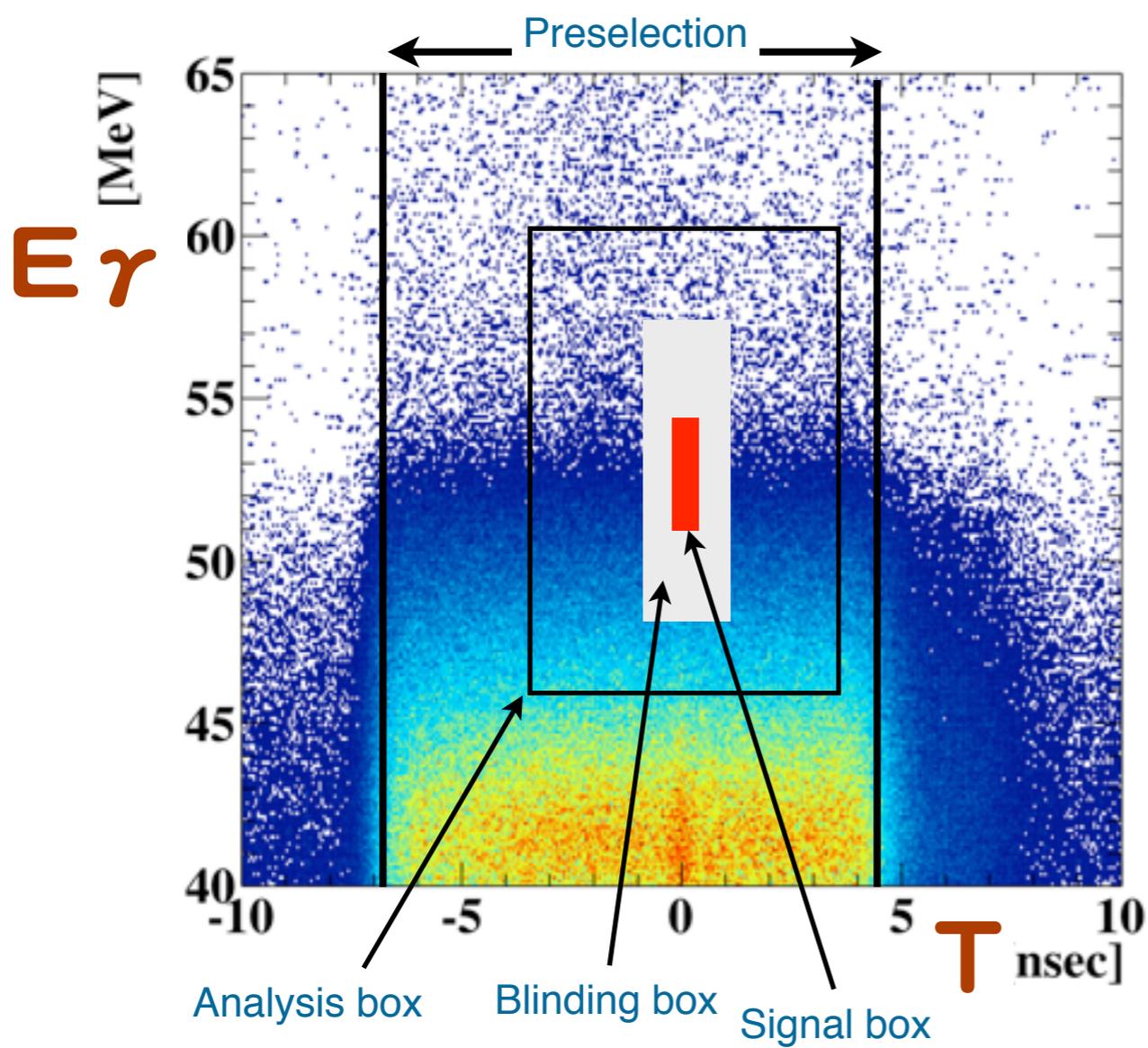
→ next talk

- Several calibration trigger data were mixed in physics runs, with each pre-scaling factor

* including 15% of calibration events.

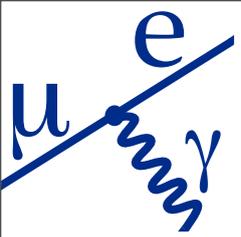
Analysis procedure

All pre-selected events
 (No selection by E_{e^+} , ϕ and θ)



- Final analysis is done for pre-selected 3.7 M events (20% of recorded events).
- Blinding analysis (T and E_γ) to avoid experimenter's bias.
- Analysis was tuned, and background spectrums were obtained from sideband data.
- Unblinded the box after fixing analysis and, selection criteria, chose of tools.

Pre-selection : T [-6.9, 4.4] nsec && at least one e^+ track associated with trigger.
 Blind box : T [-1, 1] nsec, E_γ [48, 57.6] MeV
 Analysis box : T [-1, 1] nsec, E_γ [46, 60] MeV
 (T [-3.5,3.5] nsec is used for sideband studies)



Estimation of branching ratio

Number of signals (Numerator)

Event quality cut for gamma(acceptance, partial pileup cut, CR cut) and positron(track fitting uncertainty, matching between DCH and TC...).

Selection of analysis event with E_γ , E_{e^+} , T , ϕ and θ .

Fitting distribution of E_γ , E_{e^+} , T , ϕ and θ , with **Signal** + **RMD** + **BG** probability density function(PDF).

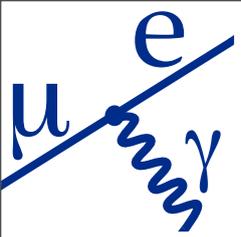
Number of observed muons [Denominator]

Same event quality cut.

Counting number of muons by using Michel positrons, which was taken in parallel with physics data.

Scaling by difference of several efficiencies between **Michel** and **Signal**.

Branching Ratio



Number of signals [Numerator]

Event quality cut for gamma(acceptance, partial pileup cut, CR cut) and positron(track fitting uncertainty, matching between DCH and TC...).

Selection of analysis event with E_γ , E_{e^+} , T , ϕ and θ .

Fitting distribution of E_γ , E_{e^+} , T , ϕ and θ , with **Signal** + **RMD** + **BG** probability density function(PDF).

Number of observed muons [Denominator]

Same event quality cut.

Counting number of muons by using Michel positrons, which was taken in parallel with physics data.

Scaling by difference of several efficiencies between **Michel** and **Signal**.

Branching Ratio

μ e
 m_γ

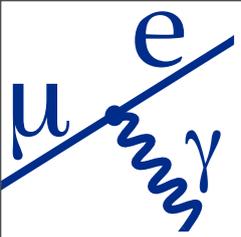
Maximum likelihood fitting

$$\mathcal{L}(N_{\text{sig}}, N_{\text{RMD}}, N_{\text{BG}}) \\ = \frac{N^{N_{\text{obs}}} \exp^{-N}}{N_{\text{obs}}!} \prod_{i=1}^{N_{\text{obs}}} \left[\frac{N_{\text{sig}}}{N} S + \frac{N_{\text{RMD}}}{N} R + \frac{N_{\text{BG}}}{N} B \right]$$

- Fitting 5 dimensional event distribution with three PDFs
- **BG** (accidental background)
- **RMD** (radiative muon decay)
- **Signal**
- PDFs are obtained mostly from data.
- Event-by-event PDF to take into account position or time dependent change of response.
- **RMD** PDF is made from theoretical **RMD** shape \otimes detector response function.

$E e^+ E \gamma$

$T \phi \theta$



PDF - Gamma energy

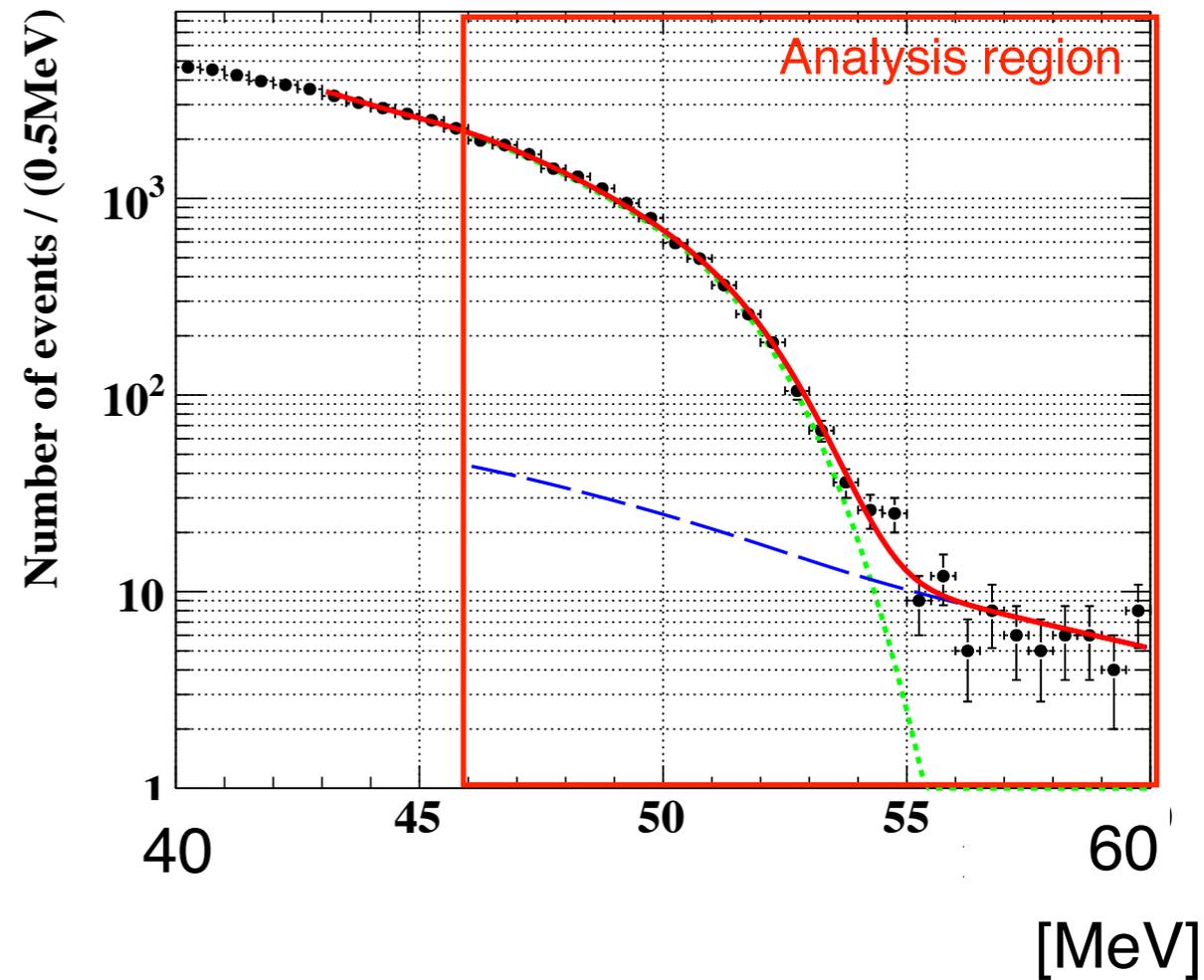
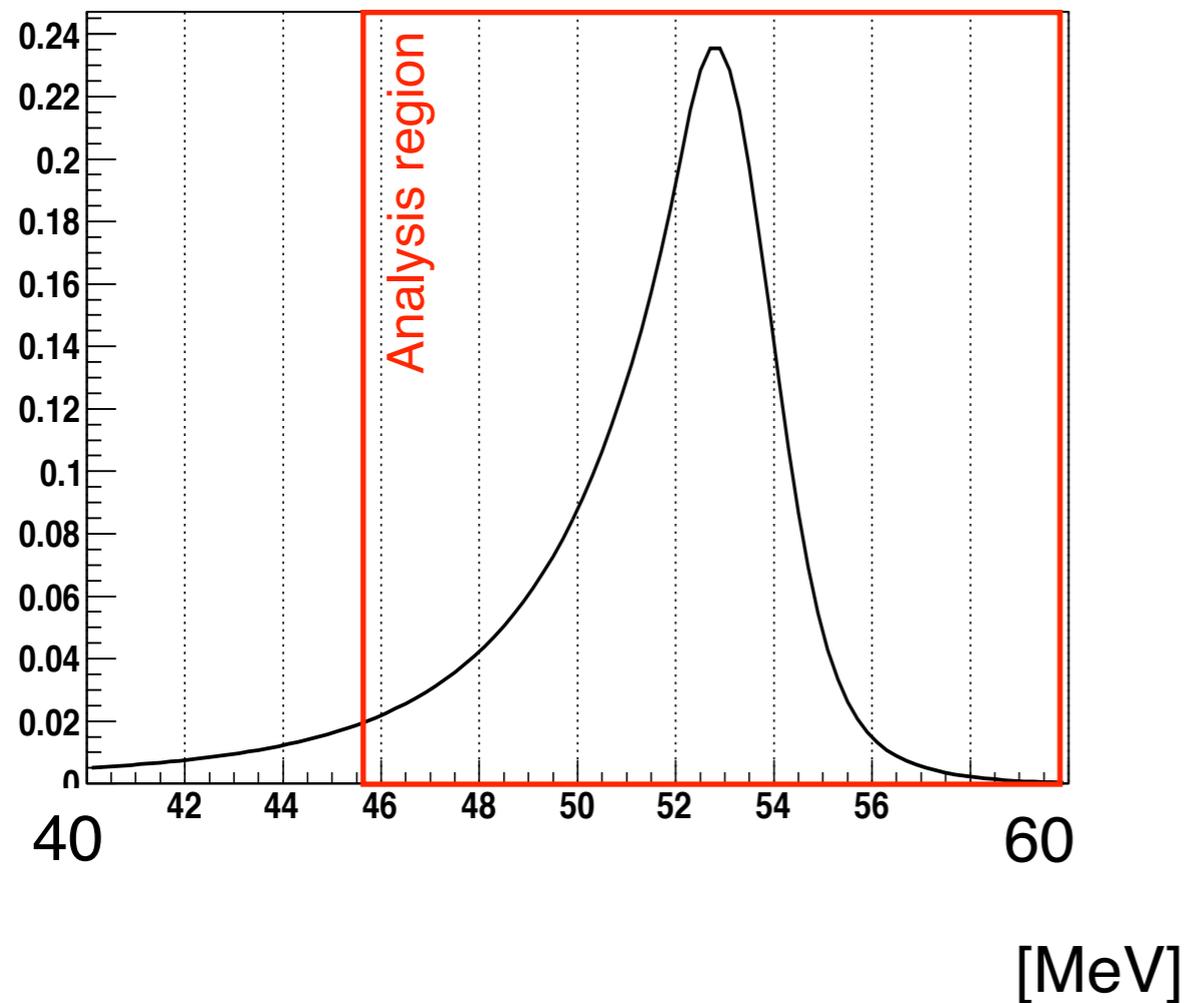
E_γ

Signal

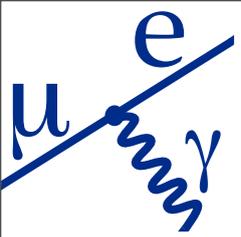
BG

Response from π beam test *

Fitting muon sideband data



* Average response is shown (including shallow events). Actual fitting is done PDF for each position.



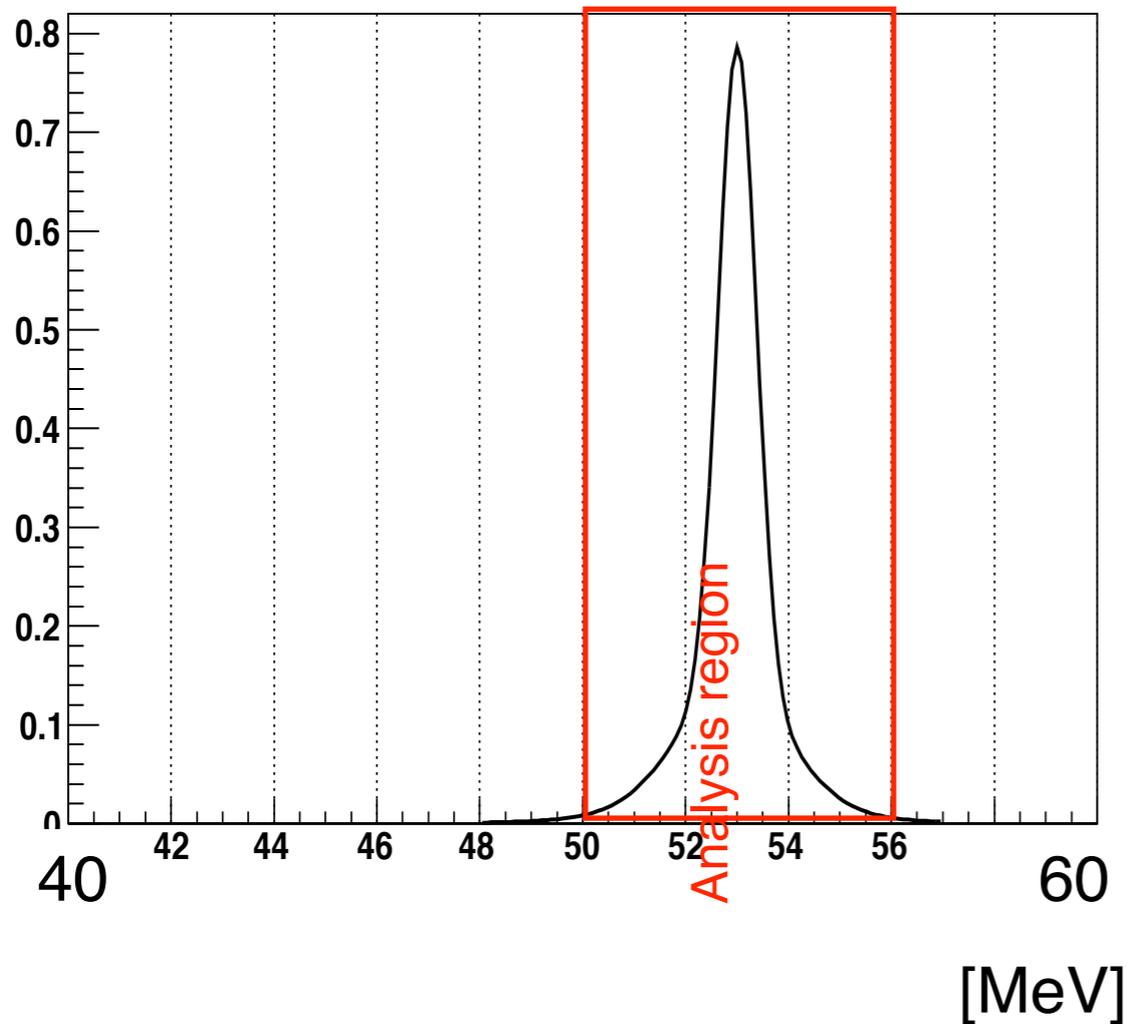
PDF - Positron energy

E_{e^+}

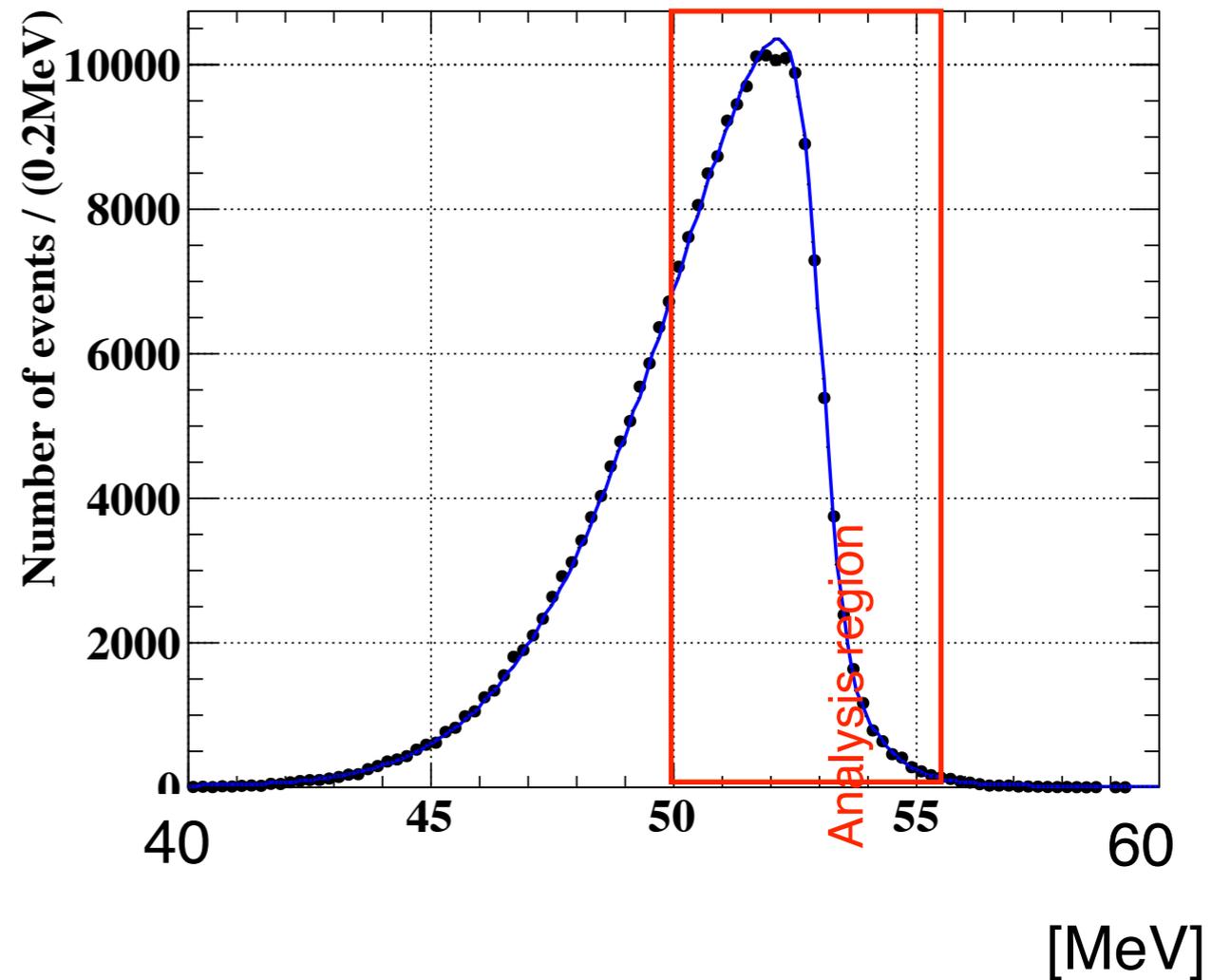
Signal

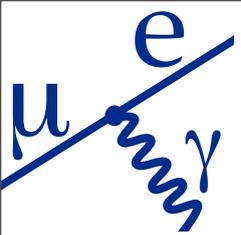
BG

Response function with Michel fit parameters



Fitting Michel spectrum

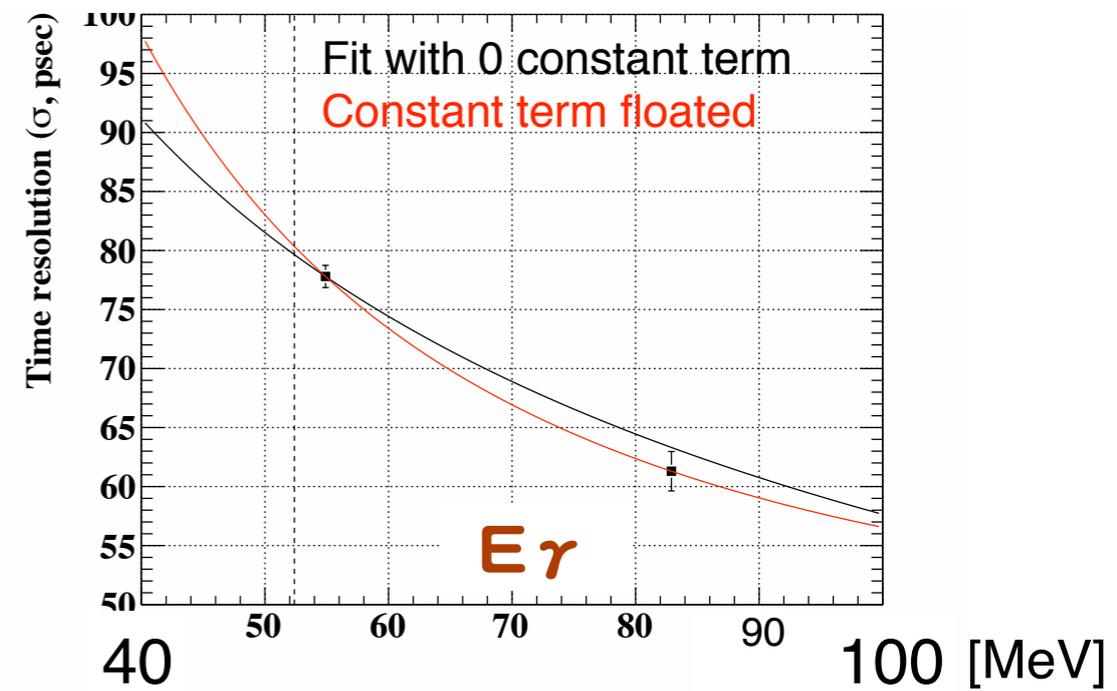
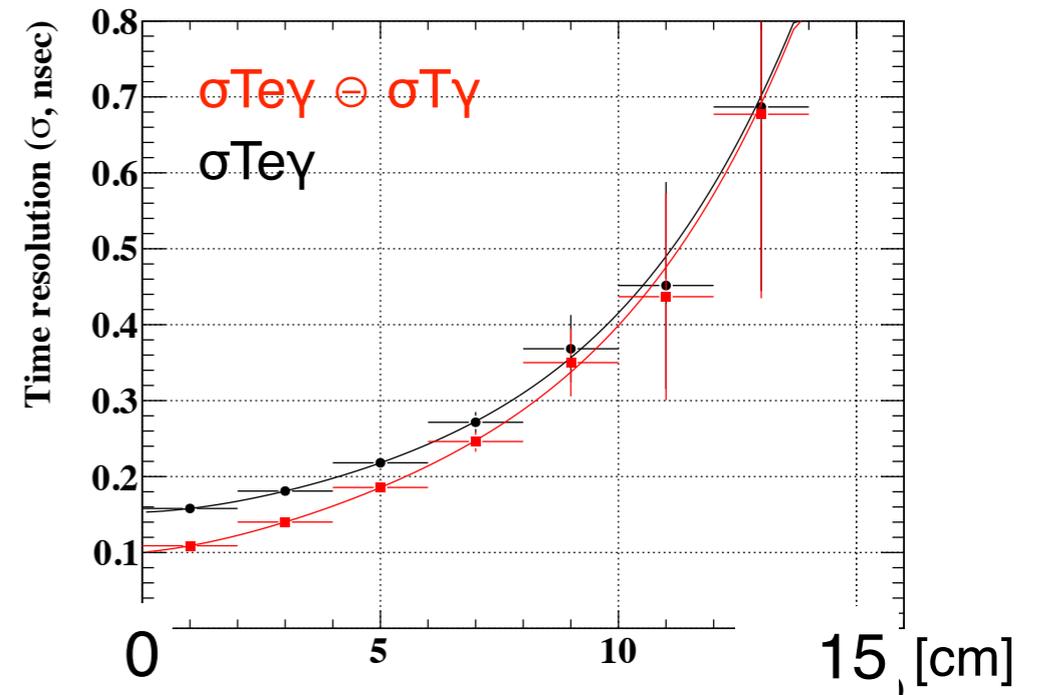
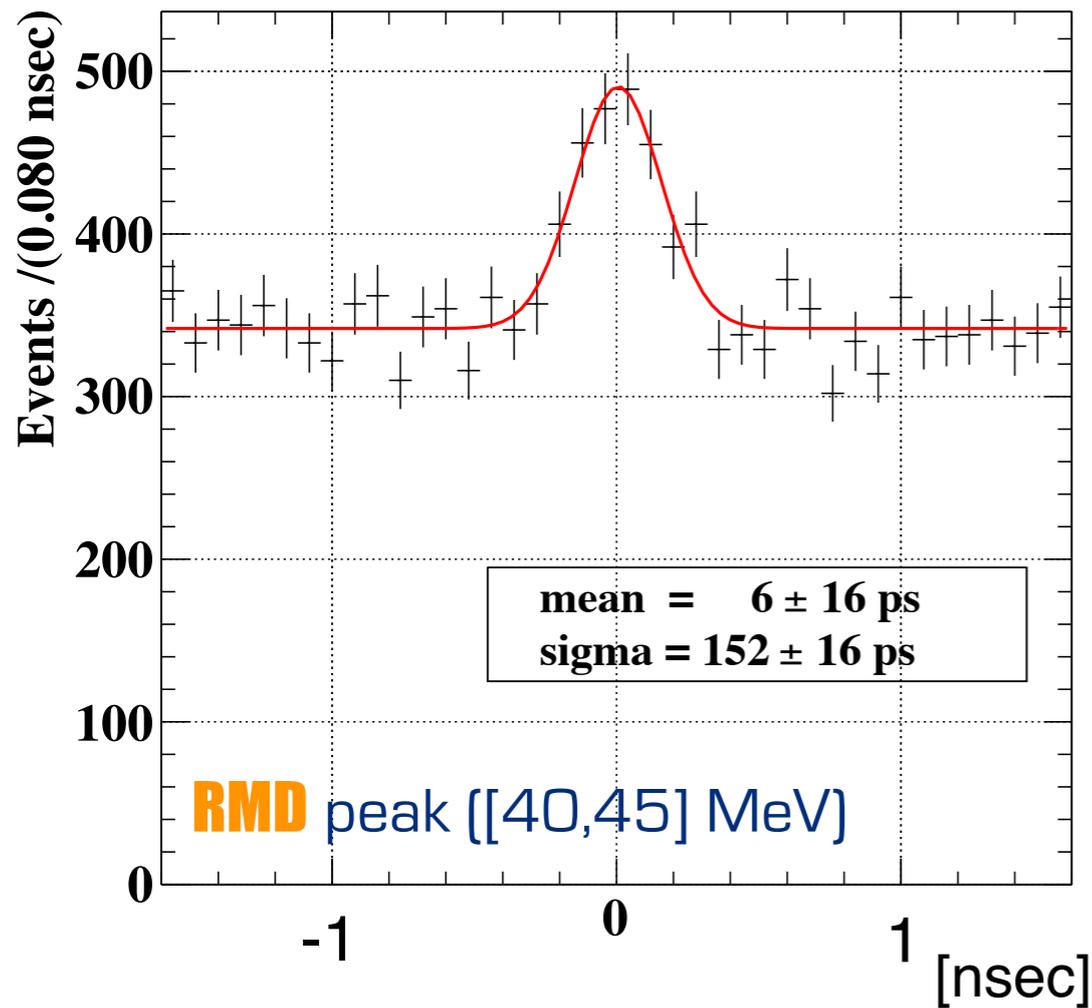




PDF - Time difference

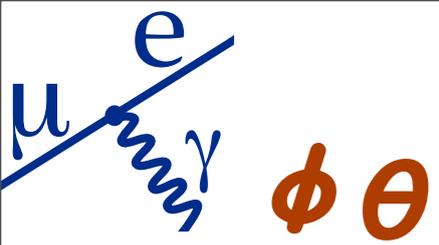
T **Signal**

- Resolution of low γ energy **RMD** peak
- Extrapolation to signal energy by known relation from π beam test.
- Event-by-event PDF as a function of ΔZ .*



BG : flat

* Difference of z hit position between TC reconstruction, and extrapolation of DC tracking.

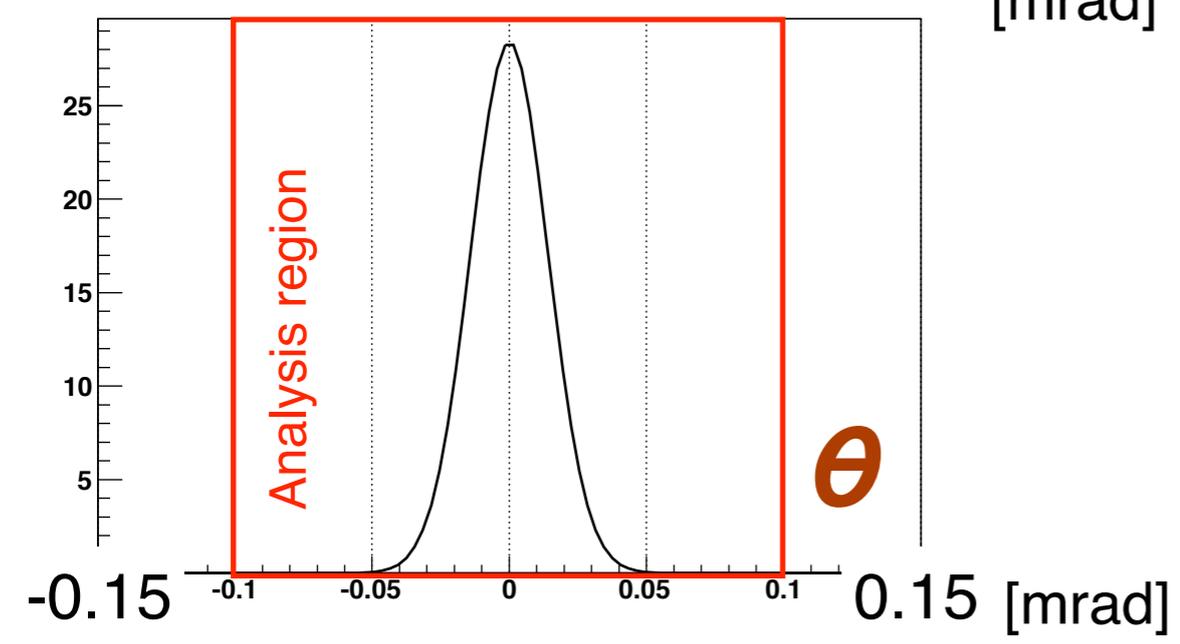
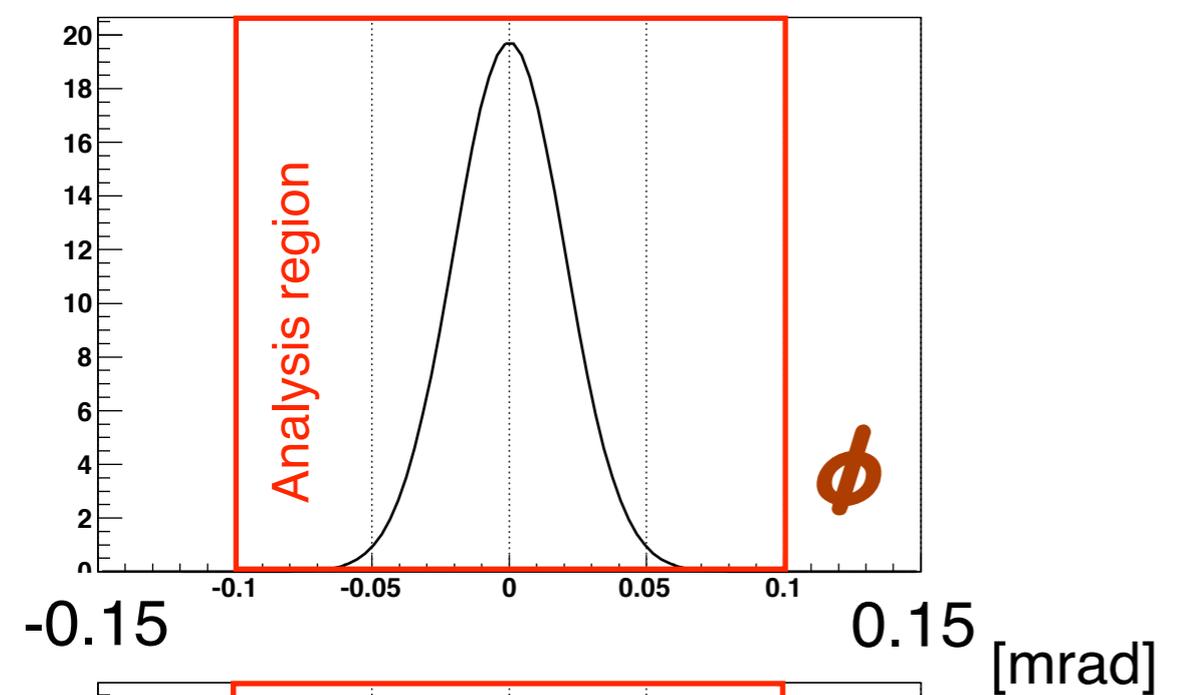


PDF - Opening angle

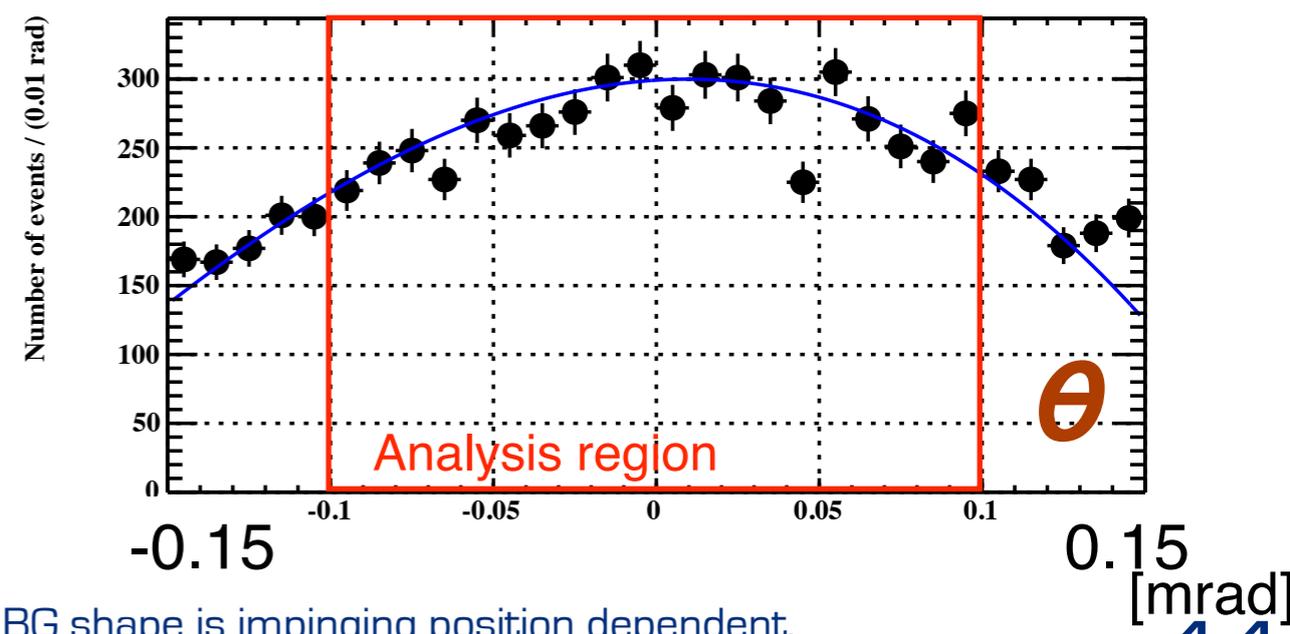
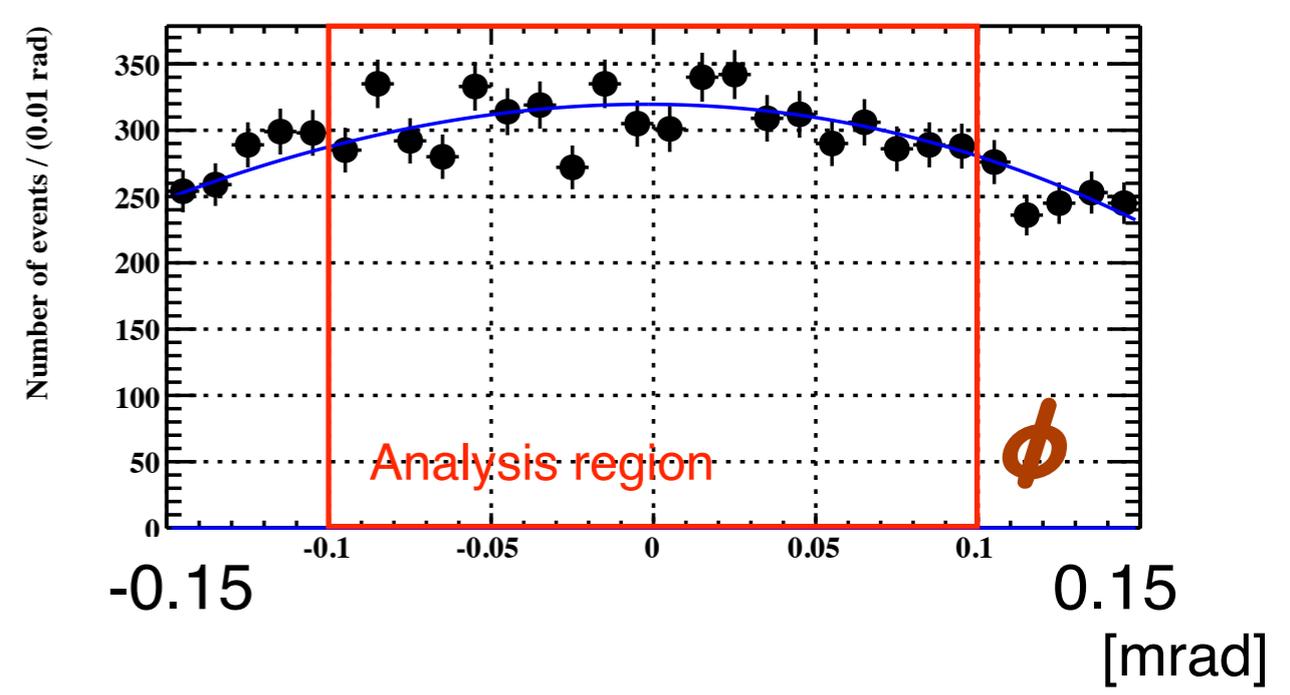
Signal

BG

e^+ resolution : from double turn events
 γ resolution : π beam test, collimator run



Measured distribution of sideband



* Average response is shown. Actual fitting is done PDF for each position. BG shape is impinging position dependent.

Sensitivity

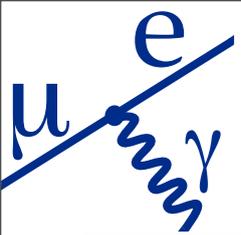
Sensitivity can be estimated by using MC based on PDF

- Sensitivity (average 90% C.L. upper limit with null signal hypothesis) is estimated by repeating the fitting for many toy-MC to be 1.3×10^{-11} .
- 90% C.L. upper of two sidebands (negative/positive T) are 0.9 . and 2.1×10^{-11} .

(Current upper limit given by MEGA in 1999 is 1.2×10^{-11})

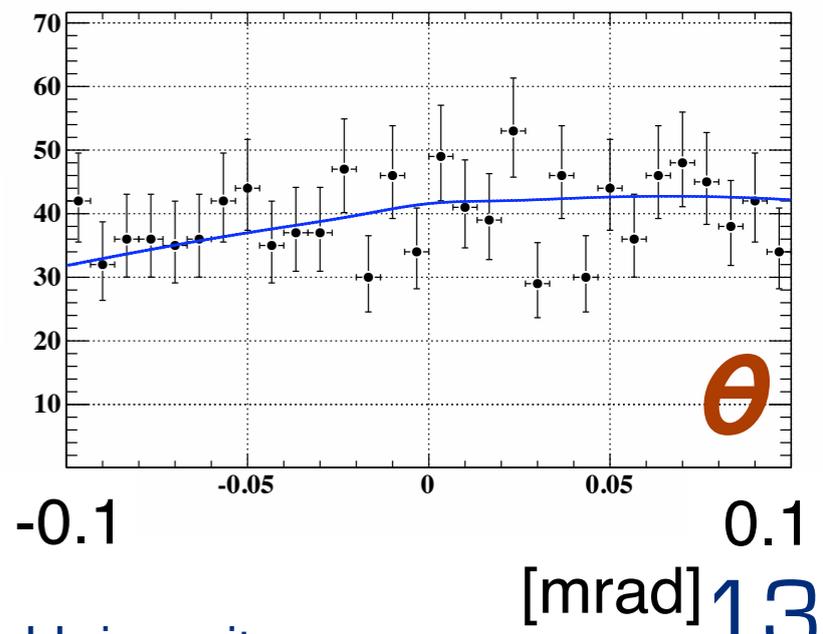
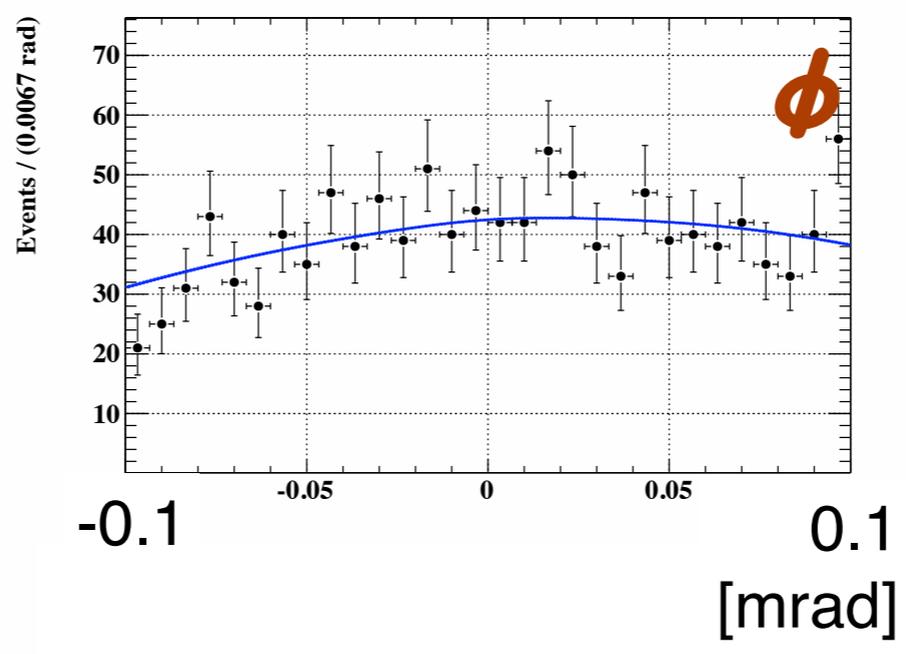
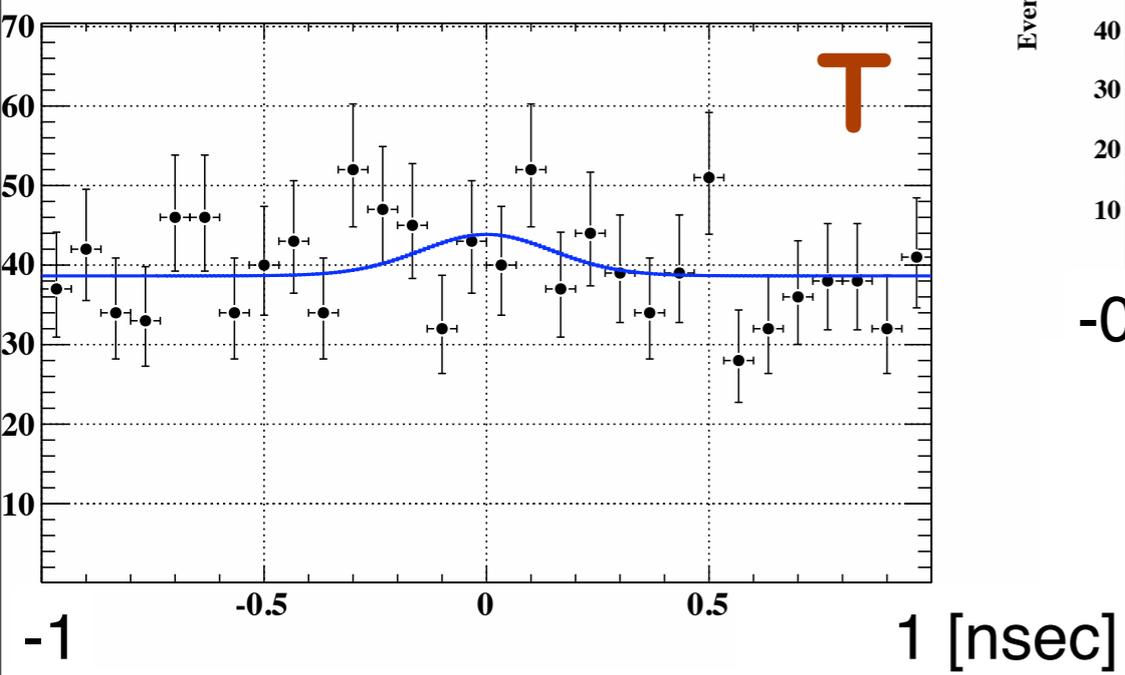
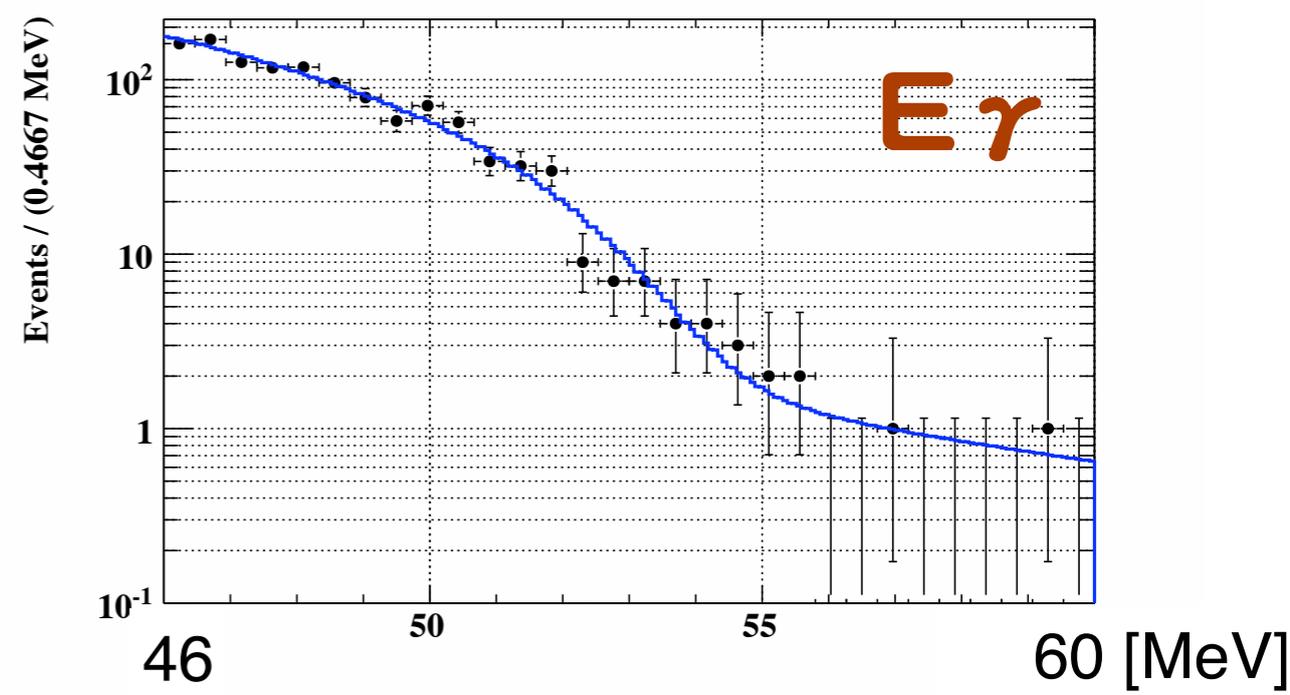
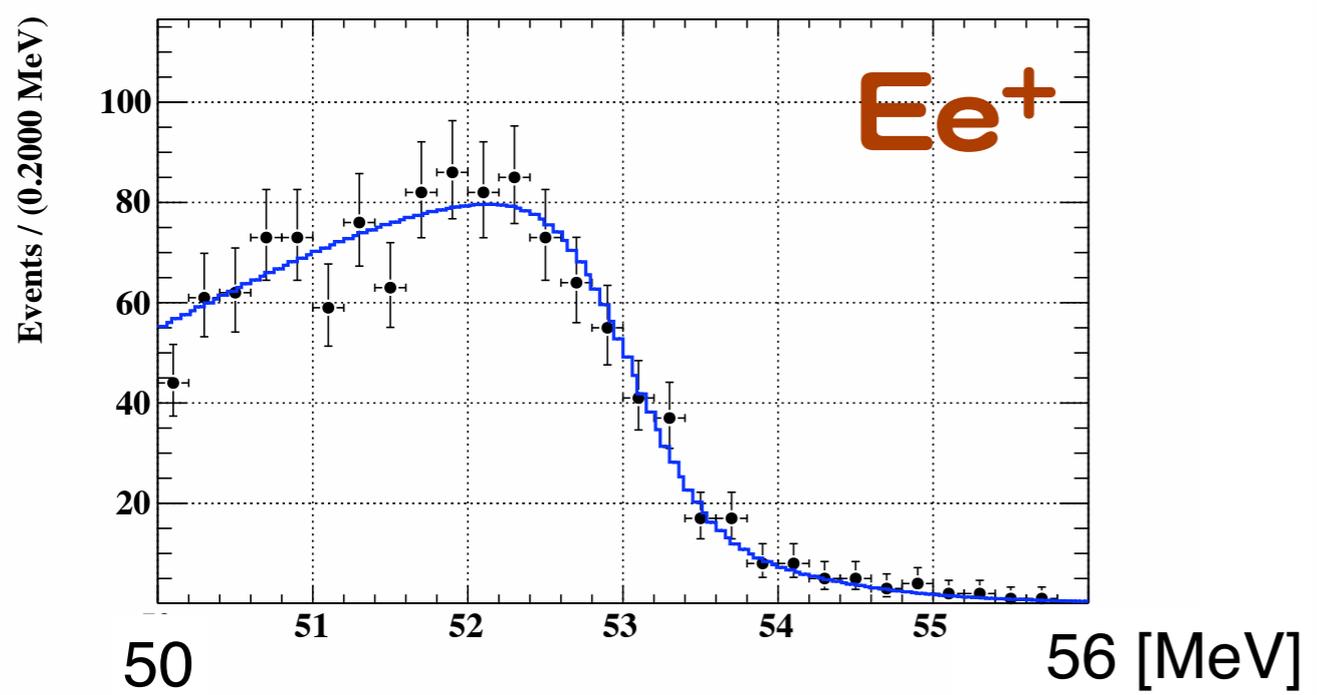
Preliminary

Normalization used for this calculation will be discussed later.



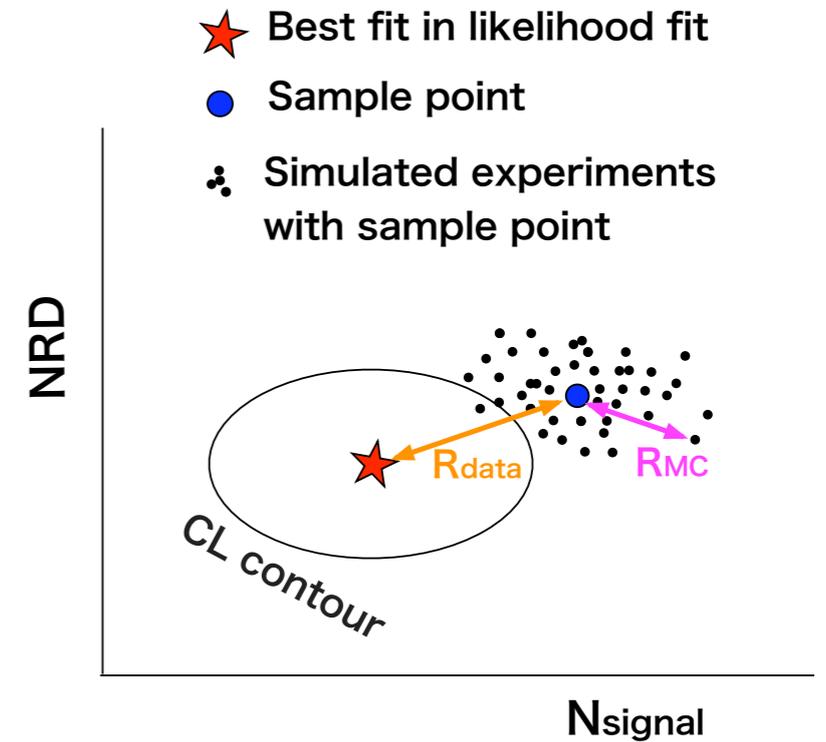
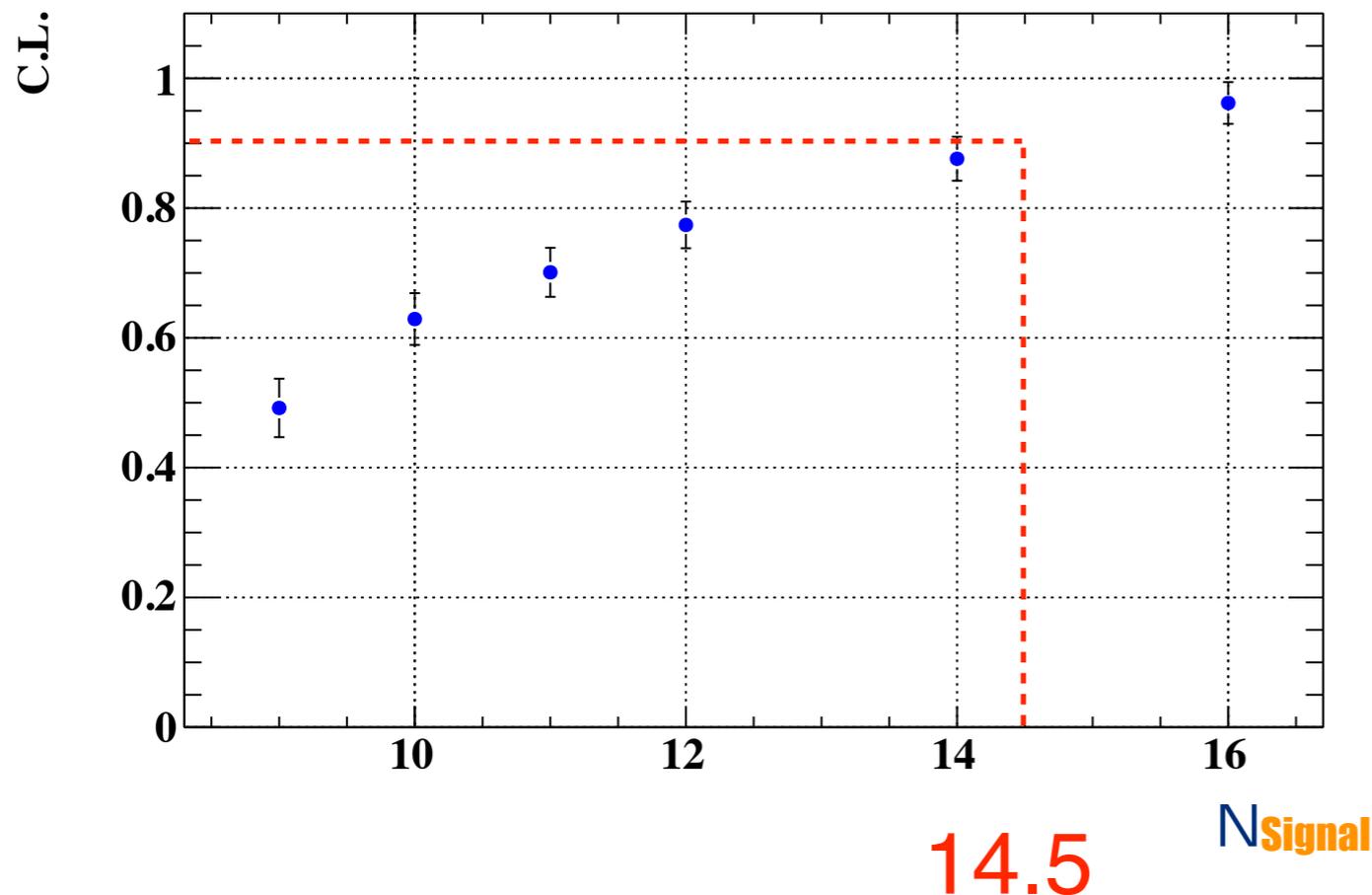
2008 data fit result

1189 analysis events



Upper limit

90% C.L contour set by means of Feldman-Cousins approach.

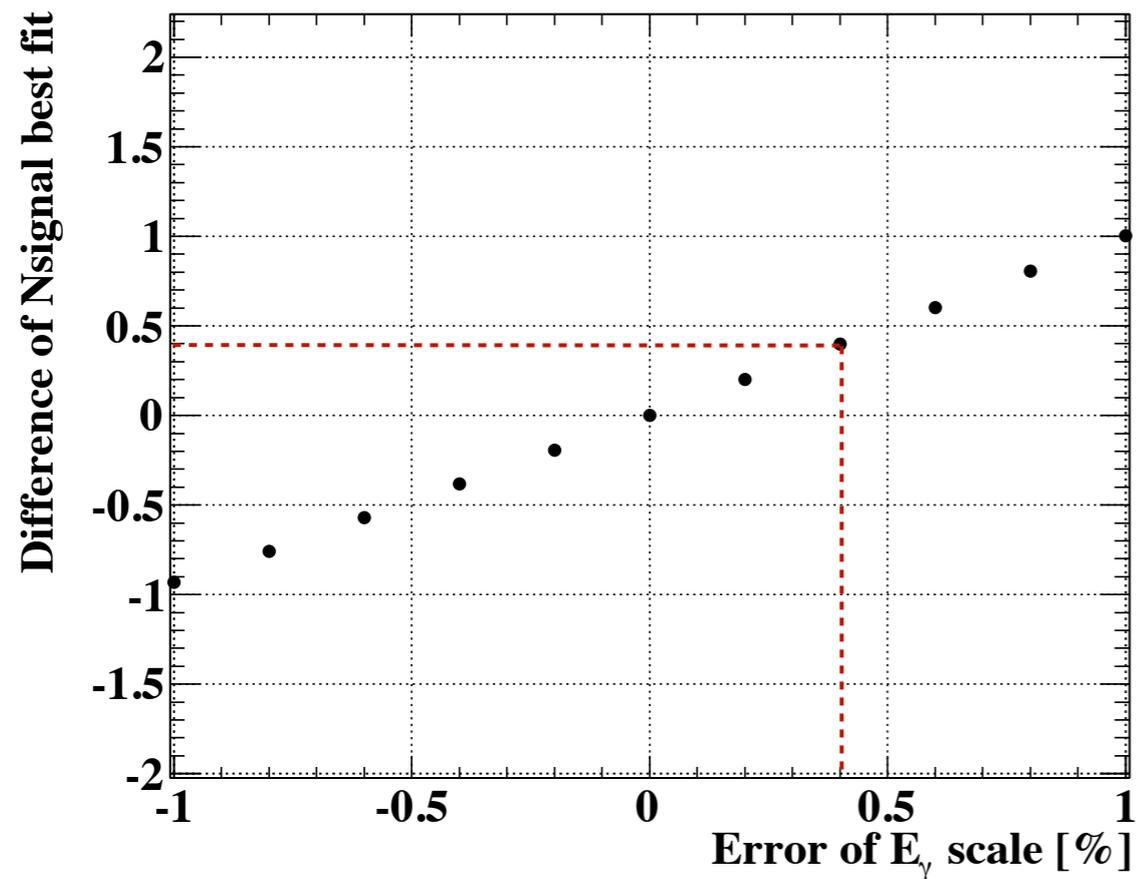


- Perform many toy-MC experiments at several $(N_{\text{Signal}}, N_{\text{RMD}})$ sampling points by means of PDF.
- Compare $R_{\text{data}} = L_{\text{data,max}} / L_{\text{data}}(N_{\text{Signal}}, N_{\text{RMD}})$ and $R_{\text{MC}} = L_{\text{MC,max}} / L_{\text{MC}}(N_{\text{Signal}}, N_{\text{RMD}})$ for each simulated experiment.
- If the probability of $R_{\text{data}} < R_{\text{MC}}$ is less than 90%, the sampling point is outside of 90% C.L. contour.

Systematic errors

Systematic error is estimated by repeating fitting with using alternative parameters.

For example, on E_γ



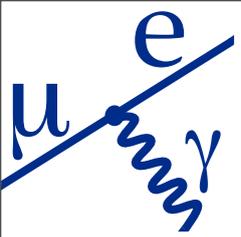
Dominant errors

E_γ scale : 0.4 events

E_{e^+} spectrum parameters : 1.1 events

Total : **1.3** events

Upper limit including systematic error = **14.7**



Number of signals (Numerator)

Event quality cut for gamma(acceptance, partial pileup cut, CR cut) and positron(track fitting uncertainty, matching between DCH and TC...).

Selection of analysis event with E_γ , E_{e^+} , T , ϕ and θ .

Fitting distribution of E_γ , E_{e^+} , T , ϕ and θ , with **Signal** + **RMD** + **BG** probability density function(PDF).

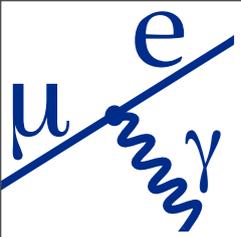
Number of observed muons [Denominator]

Same event quality cut.

Counting number of muons by using Michel positrons, which was taken in parallel with physics data.

Scaling by difference of several efficiencies between **Michel** and **Signal**.

Branching Ratio



Normalization

Signal

$$N_{sig} = N_{\mu} \times Br_{e\gamma} \times \tau_{e\gamma} \times \epsilon_{e\gamma}^{trig} \times G_{e\gamma}^{DC} \times A_{e\gamma}^{TC} \times \epsilon_{e\gamma}^{DC} \times A_{e\gamma}^{LXe} \times \epsilon_{e\gamma}^{LXe}$$

$$N_{e\nu\bar{\nu}} = N_{\mu} \times Br_{e\nu\bar{\nu}} \times \tau_{e\nu\bar{\nu}} \times \epsilon_{e\nu\bar{\nu}}^{trig} \times G_{e\nu\bar{\nu}}^{DC} \times A_{e\nu\bar{\nu}}^{TC} \times \epsilon_{e\nu\bar{\nu}}^{DC} \times f_{e\nu\bar{\nu}}^E \times P$$

Labels for the terms in the equations:

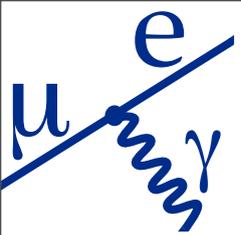
- trigger: $\tau_{e\gamma}, \epsilon_{e\gamma}^{trig}, \tau_{e\nu\bar{\nu}}, \epsilon_{e\nu\bar{\nu}}^{trig}$
- positron: $G_{e\gamma}^{DC}, A_{e\gamma}^{TC}, \epsilon_{e\gamma}^{DC}, G_{e\nu\bar{\nu}}^{DC}, A_{e\nu\bar{\nu}}^{TC}, \epsilon_{e\nu\bar{\nu}}^{DC}$
- gamma: $A_{e\gamma}^{LXe}, \epsilon_{e\gamma}^{LXe}$

Michel trigger events (>50MeV)

- #of observation
- #of stopped mu
- Branching ratio
- Live time
- Trigger efficiency
- Geometrical acceptance of DCH
- Conditional probability* of TC detection
- DC efficiency
- Conditional geometrical* acceptance of LXe
- LXe efficiency
- Fraction of >50MeV of Michel spectrum
- Trigger pre-scaling

* given an accepted positron by DC

By using Michel positrons, normalization is independent of beam rate, and insensitive to absolute positron detection efficiency.



Normalization

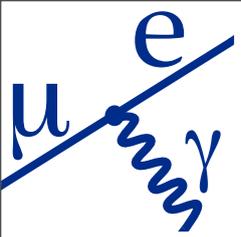
$$\begin{aligned}
 N_{sig} &= N_{\mu} \times Br_{e\gamma} \times \tau_{e\gamma} \times \epsilon_{e\gamma}^{trig} \times G_{e\gamma}^{DC} \times A_{e\gamma}^{TC} \times \epsilon_{e\gamma}^{DC} \times A_{e\gamma}^{LXe} \times \epsilon_{e\gamma}^{LXe} \\
 N_{e\nu\bar{\nu}} &= N_{\mu} \times Br_{e\nu\bar{\nu}} \times \tau_{e\nu\bar{\nu}} \times \epsilon_{e\nu\bar{\nu}}^{trig} \times G_{e\nu\bar{\nu}}^{DC} \times A_{e\nu\bar{\nu}}^{TC} \times \epsilon_{e\nu\bar{\nu}}^{DC} \times f_{e\nu\bar{\nu}}^E \times P
 \end{aligned}$$

$$BR(\mu^+ \rightarrow e^+ \gamma) = \frac{N_{sig}}{N_{e\nu\bar{\nu}}} \times \frac{f_{e\nu\bar{\nu}}^E}{P} \times \frac{\epsilon_{e\nu\bar{\nu}}^{trig}}{\epsilon_{e\gamma}^{trig}} \times \frac{A_{e\nu\bar{\nu}}^{TC}}{A_{e\gamma}^{TC}} \times \frac{\epsilon_{e\nu\bar{\nu}}^{DC}}{\epsilon_{e\gamma}^{DC}} \times \frac{1}{A_{e\gamma}^{LXe}} \times \frac{1}{\epsilon_{e\gamma}^{LXe}}$$

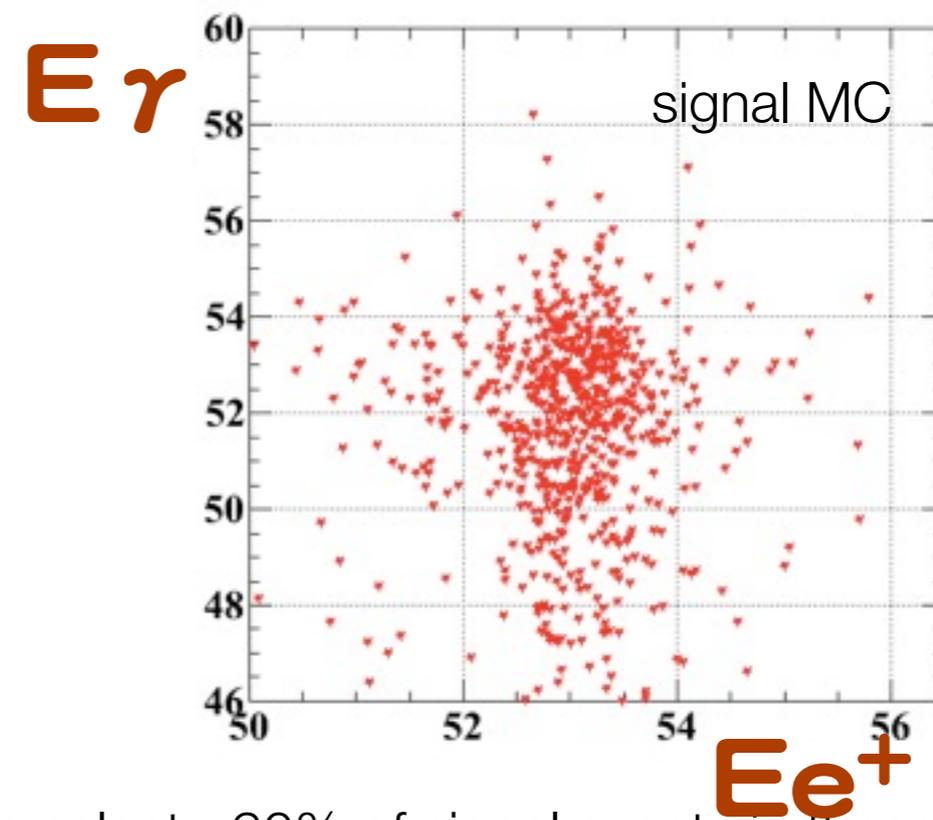
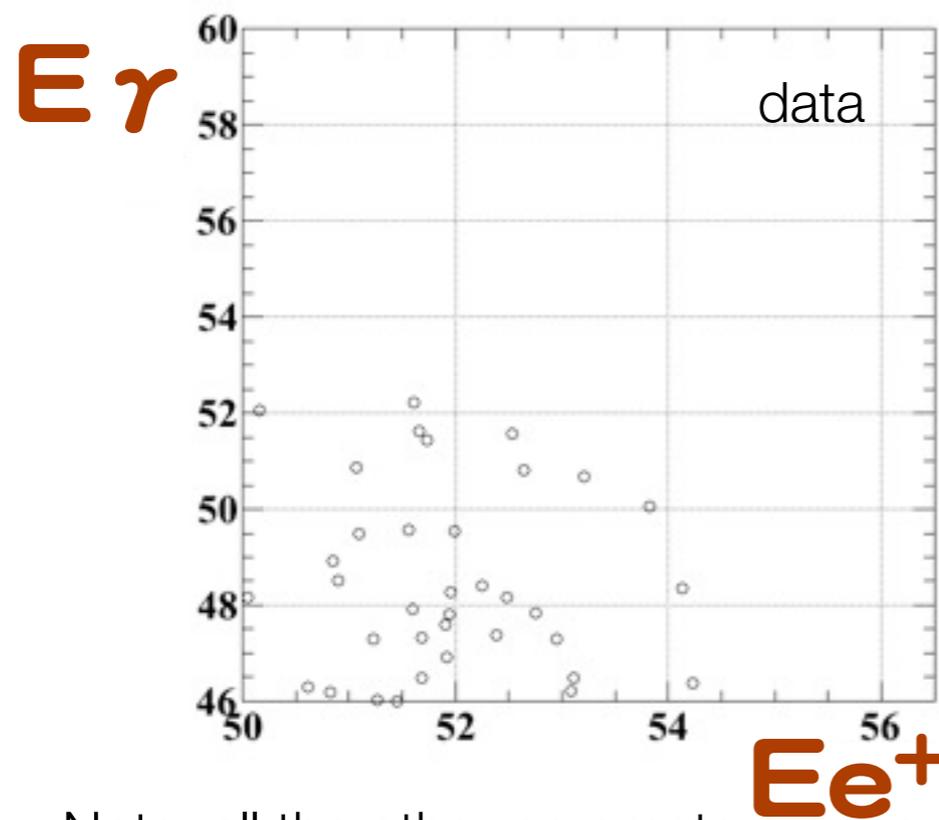
= ~1

①	# of Michel trigger events	11414
②	Fraction of Michel > 50 MeV	0.101 ± 0.006
③	trigger efficiency ratio	0.66 ± 0.03
④	DC-TC matching efficiency ratio	1.11 ± 0.02
⑤	DCH reconstruction and acceptance ratio	1.02 ± 0.005
⑥	Geometrical acceptance of LXe	0.98 ± 0.005
⑦	LXe efficiency	0.61 ± 0.03
	Normalization factor	2 ± 0.2 × 10⁻¹²

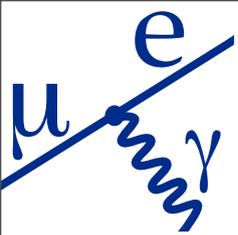
[effect of radiative decay is negligible.]



$$\text{BR}(\mu^+ \rightarrow e^+ \gamma) < 3.0 \times 10^{-11}$$



Note: all the other parameters are cut to select ~90% of signal events in these plots



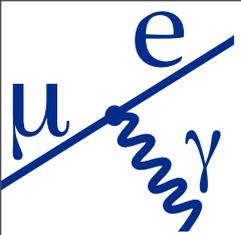
Summary

- Physics data of the first 3 months of MEG was analyzed. Because of hardware problems, statistics is much lower than expected.
- B.R. upper limit was estimated to be 3.0×10^{-11} .
- Normalization was obtained with a method insensitive to DCH efficiency.
- Maximum likelihood fitting by means of PDF based on measured response.
- Upper limit by Feldman-Cousins approach.
- 5 times improvement of sensitivity is expected in 2009. => Next talk.

<http://arxiv.org/abs/0908.2594>.

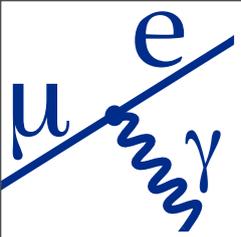
μ e
 $m\gamma$

Backup



Cross check of efficiency

$\Omega/4\pi$	0.09		
γ	0.66 x 0.91 ($E_\gamma > 46\text{MeV}$)x(pileup, CR)	4.6×10^{-3} (from BG rate, $E_\gamma > 45\text{MeV}$, $E_e > 50\text{MeV}$)	280/250 (RD sideband data, $E_e < 48\text{MeV}$, #expected / #observed)
e^+	0.15 (DCH x DC-TC match)		
Trigger	0.66 (DM)		
Selection	0.99 x 0.98 (DCH x γ acc.)		
N_μ	9.4×10^{13} μ stops ($3.0 \times 10^7 \mu/\text{s}/2\text{mA} \cdot 6290\text{C}$)		
SES	2.0×10^{-12}	2.2×10^{-12}	2.2×10^{-12}



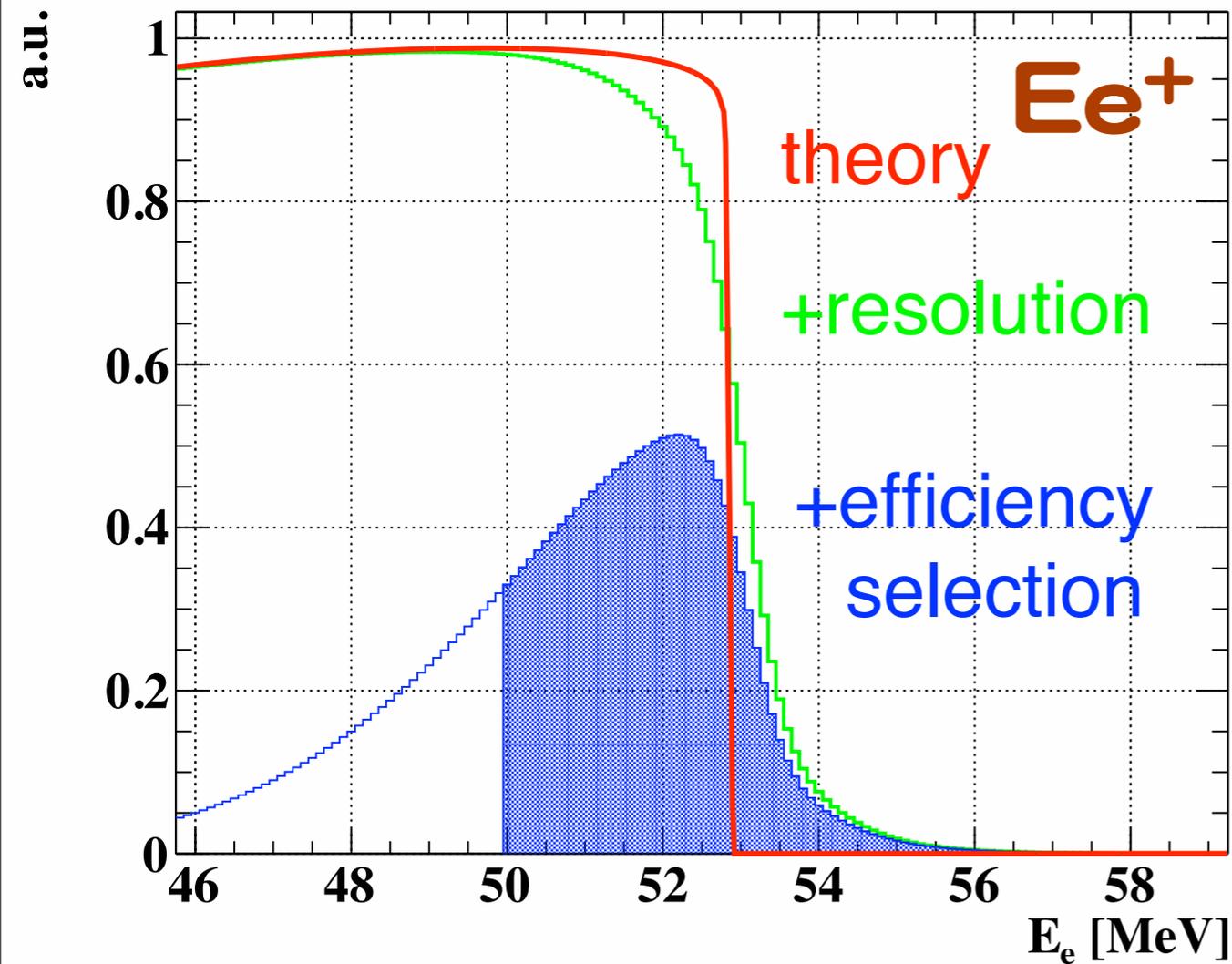
Normalization

Normalization by using Michel positrons.

Independent of beam rate, and insensitive to positron detection efficiency.

$$\text{BR}(\mu^+ \rightarrow e^+ \gamma) = \frac{N_{\text{sig}}}{N_{e\nu\bar{\nu}}} \times \frac{f_{e\nu\bar{\nu}}^E}{P} \times \frac{\epsilon_{e\nu\bar{\nu}}^{\text{trig}}}{\epsilon_{e\gamma}^{\text{trig}}} \times \frac{A_{e\nu\bar{\nu}}^{\text{TC}}}{A_{e\gamma}^{\text{TC}}} \times \frac{\epsilon_{e\nu\bar{\nu}}^{\text{DC}}}{\epsilon_{e\gamma}^{\text{DC}}} \times \frac{1}{A_{e\gamma}^{\text{LXe}}} \times \frac{1}{\epsilon_{e\gamma}^{\text{LXe}}}$$

= ~1



μ e
 m_γ

NRD fit result

- data 25^{+17}_{-16}
- Expected 40 ± 8

